## KARIMPUR PANNADEVI COLLEGE

MATHEMATICS Programme Course (Second Semester)

Assignment for  $1^{st}$  Internal Assessment, 2019

## Full Marks: 20

Answer all Questions

Q.1) Solve the differential equation: 
$$\frac{d^2y}{dx^2} + a^2y = \sec ax$$
 5 marks

Q.2) Solve by the method of variation of parameters: 
$$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = \frac{e^{-x}}{x^2}$$
 5 marks

Q.3) Solve: 
$$x^3 \frac{d^3y}{dx^3} + 3x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + 8y = 65 \cos(\log x)$$
 5 marks

Q.4) Find the eigenvalues and the eigen functions of  $\frac{d}{dx}\left(x\frac{dy}{dx}\right) + \frac{\lambda}{x}y = 0$  ( $\lambda > 0$ ) under the boundary conditions y(1) = 0 and  $y(e^{\pi}) = 0$ . 5 marks